## Tutorial 5 : $\omega$-Regular Languages \& Büchi automata

## CS60030 Formal Systems

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## Equivalence checking

For each of the following pairs, determine if they are equivalent. If not, provide a counterexample

1. $\mathrm{G}(\mathrm{A} \rightarrow \mathrm{B}) \equiv(\mathrm{GA} \rightarrow \mathrm{GB})$
2. $\left(A^{*} B\right)^{\omega}$ and $A^{*} \cdot B^{\omega}$
3. $\mathrm{GFp} \rightarrow \mathrm{GFq} \equiv \mathrm{G}(\mathrm{p} \rightarrow \mathrm{Fq})$
4. $(A+B) \cdot C^{\omega} \equiv A \cdot C^{\omega}+B \cdot C^{\omega}$
5. $\quad$ FGp $\wedge F G q \equiv \operatorname{FG}(p \wedge q)$
6. $p U(q U r) \equiv r \vee((p \vee q) \wedge(p U(q U r))$
7. $\quad\left(A^{*}+B . C\right)+.\left(C . C^{*}\right)^{\omega}$ and $\left(A^{*}+B . C\right)+.(C)^{\omega}$

## $\omega$-Regular Languages

Write the $\omega$-Regular Language for the following sentences:

1. $A$ and $B$ always alternate starting with $A$. This means only $A$ is true in the first step, then only $B$ is true in the next step, and this alternation between $A$ and $B$ is always repeated.
2. Between two neighboring A's there is at least one $B$.
3. Never is it that an $A$ is followed by a $B$ unless the $A$ is preceded by a $C$
4. If at some point $C$ holds and at all points before it $A$ did not hold and $B$ held, then at some point after $C, A$ and $B$ both hold.

## NBA CONSTRUCTION

Construct NBA for the following properties/expressions

1. $\left(A^{*} C\right)^{\omega}$
2. $(A B+C)^{*}((A A+B) C)^{\omega}$
3. Between two neighboring A's there are odd no. of B's
4. If A occurs, it occurs consecutively in multiples of three
5. $\left(A^{*} C A+B B\right)^{*}(A+C C)^{\omega}$

## GNBA TO NBA

Draw the NBA for the following GNBA, where $F=\{\{q 1\},\{q 2\}\}$.


